# **Exploring Applications of State Space Models and Advanced Training Techniques in Sequential Recommendations**



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**Equal contribution** 



# **USGM adaptive method**

The authors of the original paper consider an upper bound for the stochastic approximation of the symmetrized Bregman distance for points  $x_k$  and  $x_{k+1}$  ( $\hat{\beta}_{k+1}$ ) as follows:

 $\hat{\beta}_{k+1} = \langle f'(x_{k+1}) - f'(x_k) + \Delta_{k+1}, x_{k+1} - x_k \rangle \leq L$ (1.3) where  $f'(x_k) := \mathbb{E}_{\xi_k}[g_k] \in \partial f(x_k), \ \Delta_{k+1} :=$  $\delta_{k+1} - \delta_k$  with  $\delta_k := g_k - f'(x_k)$  being the error of the stochastic gradient (such that  $\mathbb{E} \|\delta_k\|^2 \leq$  $\sigma^2$ ), and  $\sigma_{k+1} := ||\Delta_{k+1}||$ .

**Algorithm** Universal Stochastic Gradient Method 1: **Initialize:**  $x_0 \in$  dom  $f$ ,  $D > 0$ ,  $H_0 :=$ 0,  $g_0 \sim \hat{g}(x_0)$ . 2: **for**  $k = 0, 1, ...$  **do**  $x_{k+1} = \arg \min_{x \in \text{dom } f} \{ \langle g_k, x \rangle +$ *H<sup>k</sup>*  $\frac{H_k}{2} \| x - x_k \|^2 \}.$ 4:  $g_{k+1} \sim \hat{g}(x_{k+1}).$ 5:  $H_{k+1}:=H_k+$  $\left[\hat{\beta}_{k+1} - \frac{1}{2}H_k r_{k+1}^2\right]_+$  $D^2 + \frac{1}{2}$  $\frac{1}{2}r_k^2$ *k*+1 , 6: where  $r_{k+1} = ||x_{k+1} - x_k||$ ,  $\hat{\beta}_{k+1} =$  $\langle g_{k+1}-g_k,x_{k+1}-x_k\rangle$ . 7: **end for**

#### **Notation:**

As the coefficient  $\hat{\beta}_{k+1}$  is computed on every iteration of the algorithm, and the batch size is known. We can use the Weighted Least Squares method (with loss defined by the equation [2.2\)](#page-0-2) in linearized axes  $(\frac{1}{\sqrt{2}})$ *B* as the X axis and the  $\hat{\beta}_{k+1}$  as the Y axis) to compute the values of  $L_{\nu} r_{k+1}^{1+\nu}$  and  $\sigma_{k+1} r_{k+1}$ . The intercept and the slope of the linearized function respectively.

# **Adaptive batching**

where *F* is the sought function  $F = c_1 + \frac{c_2}{\sqrt{d}}$ *B*  $\approx$  $\hat{\beta}_{k+1}$ , *c*<sub>1</sub> and *c*<sub>2</sub> are the values of  $L_{\nu}r_{k+1}^{1+\nu}$  and  $\sigma_{k+1}r_{k+1}$  respectively, predicted by the WLS algorithm. The value of alpha was empirically set to  $\alpha = 0.01$ , s.t. the first points almost diminish.

When the epoch ends, we lower the batch size  $(B_i :=$  $\bar{B_{i-1}}_k$  $\frac{1}{\lambda}$ ), since the perfect batch size

In stochastic optimization, the variance of the gradient estimates reduces as the batch size increases. Specifically, the variance decreases proportionally to  $\frac{1}{B}$ . Concurrently, the standard deviation  $(\sigma)$  of the gradient estimates decreases at the rate of  $\frac{1}{\sqrt{2}}$ *B* . From here [1.3](#page-0-0) , we can derive the equation [2.1.](#page-0-1) Thus, the variance and standard deviation of the gradient estimations

 $(B_i^*)$  could have changed since the last epoch. However, if it's bigger than  $\frac{B_{i-1,k}}{\lambda}$ , the algorithm will increase it during the next iterations. By doing so, we give the algorithm the ability to not continue training with excessive resources if the calculated batch size turns out to be too big in the current circumstances or to increase it even more if needed.

Since  $B_k := B_{k-1} + B_0$ ,  $B_k = m_k B_0$ :  $\forall k \ (m_k \in \mathbb{Z})$ . That means we can use the original Dataloader class from PyTorch ([\(4\)](#page-0-3)) wihout any modifications and take  $m_k$  batches of initial size  $(B_0)$  on each iteration.

 ${\bf odds}_\theta(y|x) =$ *Pθ*(*y*|*x*)  $1-P_{\theta}(y|x)$ 

The odds ratio of the chosen response  $y_w$  over the rejected response  $y_l$ ,  $\mathbf{OR}_{\theta}(y_w, y_l)$ , indicates how much more likely it is for the model  $\theta$  to generate  $y_w$  than  $y_l$  given input  $x$ .

> $\mathbf{OR}_{\theta}(y_w, y_l) =$  $\mathbf{odds}_{\theta}(y_w|x)$  $\mathbf{odds}_{\theta}(y_l|x)$

decreases as the batch size increases.

$$
\hat{\beta}_{k+1} \le L_{\nu} r_{k+1}^{1+\nu} + \frac{\sigma_{k+1} r_{k+1}}{\sqrt{B}}, \qquad (2.1)
$$

Hydra fully utilizes the matrix mixer framework to explore a novel bidirectional sequence mixer. To achieve linear complexity, a special class of quasiseparable matrix is considered. A matrix **M** is quasiseparable if every label element  $m_{ij}$  satisfies:

> $m_{ij} =$  $\sqrt{ }$  $\int$  $\overline{\mathcal{L}}$ −→  $\mathbf{c}^{\mathcal{I}}_i$ *i* −−→  $\overrightarrow{\mathbf{A}_{i:j}^{\times}}\overrightarrow{\mathbf{b}_{j}}, \text{ if } i > j$  $\delta_i$ , if  $i = j$  $\leftarrow$  $\dot{\mathbf{c}}_i^T$ *j* ←−−  $\mathbf{\dot{A}}^{\times}_{j:i}$ ←− **b**<sub>*i*</sub>, if  $i < j$ *,* (1)

<span id="page-0-0"></span>where each  $\delta_i$  is a scalar,  $_{i,i} \in \mathbb{R}^{N \times 1}$ , and  $_i \in \mathbb{R}^{N \times N}$ . Quasiseparable matrices can be used as matrix mixers. This framework is called **Hydra**, which achieves  $O(L)$  complexity.

$$
L = \sum_{k=0}^{K} (F(c_1, c_2, B_k) - \hat{\beta}_{k+1})^2 \cdot (1 - \alpha)^{K-k},
$$
\n(2.2)

## **Batch size properties**

<span id="page-0-1"></span>Where  $W^{(1)} \in \mathbb{R}^{D \times 4D}$ ,  $W^{(2)} \in \mathbb{R}^{D \times 4D}$ ,  $b^{(1)} \in \mathbb{R}^{D}$  are parameters of two dense layers and we use the GELU activation.

The objective function of ORPO consists of two components: 1) supervised fine-tuning (SFT) loss  $(\mathcal{L}_{SFT}); 2)$  relative ratio loss  $(\mathcal{L}_{OR}).$ 

 $\mathcal{L}_{ORPO} = \mathbb{E}_{(x,y_w,y_l)} [\mathcal{L}_{SFT} + \lambda \cdot \mathcal{L}_{OR}]$  (5)

## **Main contributions**

We created a pair data set, where each pair consists of a winner and a loser. It consists of 2 parts. The first part was created from the last 2 items from the user history where the winner is the item with the higher rating and the loser is the opposite. To create the second part, we used negative sampling training LightFM model and took the last user's movie as the winner and the worst recommendation of LightFM as the loser.

### ⋄ **New SOTA sequential recomendation model**

- ⋄We applied quasiseparable mixer framework on the case of sequential recommendations. The SOTA sequential recommendation model has been obtained.
- $\diamond$ We examined various applications of selected spaces to the sequential recommendation problem..
- ⋄ **Advanced training and optimization techniques.**
	- $\diamond$  ORPO preference optimization application to LLM recommedner systems ⋄ First USGM based(**?** ) method with non-emperical adaptive batch size choice.

For the ORPO procedure we used  $r = 8e-6$ , ORPO we used very low learning rates compared to traditional SFT or even DPO. This value of 8e-6 comes from the original paper.  $beta = 0.1$  An appendix from the original paper shows how it's been selected with an ablation study. We have used paged adamw optimizer with gradient accumulation steps = 4. We have trained model for 1 training epoch and evaluated every 0.2 steps, also we set warmup steps to 10. We have used linear scheduler type. Other parameters are dependent on capabilities of your resources. Training was conducted on 1 A100 80GB videocard.

## **Hydra4Rec framework**

## **Architecture and matrix mixers**

To apply the sequence-to-sequence potential of the Hydra block [\(2\)](#page-0-4), we provide a custom Hydra layer that combines the Hydra block with a standard feed-forward network. The main part of our standard architecture consists of Hydra layers. We have found that Hydra layers work more effectively than standard Mamba layers in several cases. Then, we use the same PFFN that was introduced in Mamba4Rec.[\(3\)](#page-0-5)

 $PFFN(H) = GELU(HW^{(1)} + h^{(1)})W^{(2)} + b^{(2)}$ 



Figure: Hydra4Rec architecture

<span id="page-0-2"></span>**Such framework provide us significant latency boost!**

**Monolitic No Reference Model Optimization**

## **ORPO application**

Odds Ratio Preference Optimization (ORPO), [\(1\)](#page-0-6) - is a novel preference optimization framework that consolidates an odds ratio-based penalty. The odds of generating the output sequence *y* from a given input sequence *x* are defined by:

$$
\log P_{\theta}(y|x) = \frac{1}{m} \sum_{t=1}^{m} \log P_{\theta}(y_t|x, y < t)
$$
\n(2)

(3)

(4)

## **ORPO Expiremental Setup**

## **Experiments**

It is evident that Hydra shows metrics that are similar, sometimes better to those of Mamba, but its latency is four to five times lower. Simultaneously, models such as LlamaRec exhibit superior per- formance. However, their substantial parameter count may constrain their applicability in real-world situations. Metrics-wise and latency-wise, SSM-based models outperform the baseline SASRec model on average. According to the study, SSMs can outperform LLMs while still operating at a greater speed since they require less number of parameters.

Table: Amazon Reviews '23 Video Games



## **Training process experiments**

Since the number of iterations of the algorithm with adaptive batching and of those, with which it was compared, differs, since the equality  $N_{\text{iterations}} = \frac{\text{Dataset size}}{\text{Batch size}}$  $\frac{\text{Distance}}{\text{Batch size}} = const$  is not true for the proposed algorithm, a scaled measure, which is proportional to the epoch number is used as the X axis in the comparison plot, displayed in

the Figure 1.

Figure: USGM with adaptive batching

ORPO procedure improvement is also pretty

 $References$ 

<span id="page-0-6"></span>[1] J. Hong, N. Lee, and J. Thorne. Orpo: Monolithic preference optimization without reference model, 2024.

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<span id="page-0-5"></span>[3] C. Liu, J. Lin, J. Wang, H. Liu, and J. Caverlee. Mamba4rec: Towards efficient sequential recommendation with selective state space models, 2024.

<span id="page-0-3"></span>[4] A. Paszke, S. Gross, F. Massa, A. Lerer, J. Bradbury, G. Chanan, T. Killeen, Z. Lin, N. Gimelshein, L. Antiga, A. Desmaison, A. Köpf, E. Yang, Z. DeVito, M. Raison, A. Tejani, S. Chilamkurthy, B. Steiner, L. Fang, J. Bai, and S. Chintala. Pytorch: An imperative style, high-performance deep learning library, 2019.